1.9 1.2 3.6 0.5 0.9 6.8 Find the Fourier transform of  $f(x) = \begin{cases} a^2 - x^2, & |x| \le a \\ 0, & |x| > a \end{cases}$  and hence deduce  $\int_{0}^{\infty} \frac{\sin x - x \cos x}{x^3} dx = \frac{\pi}{4}$ . 2 a. (07 Marks) b. Find the Fourier cosine and sine transform of  $f(x) = xe^{-ax}$ , where a > 0. (06 Marks) c. Find the inverse Fourier transform of  $e^{-s^2}$ . (07 Marks) Obtain the various possible solutions of one dimensional heat equation  $u_t = c^2 u_{xx}$  by the 3 a. method of separation of variables. (07 Marks) A tightly stretched string of length | with fixed ends is initially in equilibrium position. It is b. set to vibrate by giving each point a velocity  $V_o \sin\left(\frac{\pi x}{l}\right)$ . Find the displacement u(x, t). (06 Marks) Solve  $u_{xx} + u_{yy} = 0$  given u(x, 0) = 0, u(x, 1) = 0, u(1, y) = 0 and  $u(0, y) = u_0$ , where  $u_0$  is a constant. (07 Marks) Using method of least square, fit a curve  $y = ax^{b}$  for the following data. (07 Marks) 3 4 X 1 2 5 0.5 2 4.5 8 12.5 Solve the following LPP graphically: B. Minimize Z = 20x + 16ySubject to  $3x + y \ge 6$ ,  $x + y \ge 4$ ,  $x + 3y \ge 6$  and  $x, y \ge 0$ . (06 Marks) Use simplex method to c. Maximize Z = x + (1.5)ySubject to the constraints  $x + 2y \le 160$ ,  $3x + 2y \le 240$  and  $x, y \ge 0$ . (07 Marks)

**Engineering Mathematics - III** 

Third Semester B.E. Degree Examination, June/July 2013

Time: 3 hrs.

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Note: Answer FIVE full questions, selecting at least TWO questions from each part.

## PART – A

Obtain the Fourier series expansion of  $f(x) = \begin{cases} x, & \text{if } 0 \le x \le \pi \\ 2\pi - x, & \text{if } \pi \le x \le 2\pi \end{cases}$ and hence deduce

that 
$$\frac{\pi^2}{8} = \frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$$

(07 Marks)

Max. Marks:100

- b. Find the half range Fourier sine series of  $f(x) = \begin{cases} x, & \text{if } 0 < x < \frac{\pi}{2} \\ \pi x, & \text{if } \frac{\pi}{2} < x < \pi \end{cases}$ (06 Marks)
- Obtain the constant term and coefficients of first cosine and sine terms in the expansion of y from the following table. (07 Marks)

IIC IC		ig tabl	<b>.</b>	S. 14			
х	0	60°	120°	180°	240°	300°	360°
17	70	72	36	0.5	0.0	68	70

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**10MAT31** 

## **10MAT31**

(07 Marks)

## PART - B

- Using Newton-Raphson method find a real root of  $x + \log_{10} x = 3.375$  near 2.9, corrected to 2. (07 Marks) 3-decimal places.
  - b. Solve the following system of equations by relaxation method: 2x + 8y - z = 24, 3x + 4y + 10z = 5812x + y + z = 31,
  - Find the largest eigen value and corresponding eigen vector of following matrix A by power method

$$\mathbf{A} = \begin{bmatrix} 25 & 1 & 2 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{bmatrix}.$$

Use  $\mathbf{X}^{(0)} = [1, 0, 0]^{\mathrm{T}}$  as the initial eigen vector.

In the given table below, the values of y are consecutive terms of series of which 23.6 is the 6 a. 6<sup>th</sup> term, find the first and tenth terms of the series. (07 Marks)

X	3	4	5	6	1	8	9	
у	4.8	8.4	14.5	23.6	36.2	52.8	73.9	

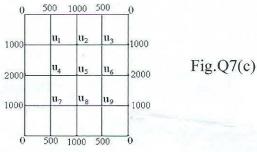
Construct an interpolating polynomial for the data given below using Newton's divided b. difference formula. (07 Marks)

Х	2	4	5	6	8	10	
f(x)	10	96	196	350	868	1746	inter la

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- Evaluate  $\int_{0}^{\infty} \frac{x}{1+x^2} dx$  by Weddle's rule taking 7-ordinates and hence find log<sub>e</sub>2. (06 Marks)
- Solve the wave equation  $u_{tt} = 4u_{xx}$  subject to u(0, t) = 0; u(4, t) = 0;  $u_t(x, 0) = 0$ ; u(x, 0) = x(4-x) by taking h = 1, k = 0.5 upto four steps. (07 Marks)
  - Solve numerically the equation  $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$  subject to the conditions  $u(0, t) = 0 = u(1, t), t \ge 0$ b. and  $u(x, 0) = \sin \pi x$ ,  $0 \le x \le 1$ . Carryout computations for two levels taking  $h = \frac{1}{3}$  and  $k = \frac{1}{36}$ . (07 Marks)
  - Solve the elliptic equation  $u_{xx} + u_{yy} = 0$  for the following square mesh with boundary values C. as shown in Fig.Q7(c). (06 Marks)



Find the z-transform of: i)  $\sin h n \theta$ ; ii)  $\cosh n \theta$ . a. (07 Marks) Obtain the inverse z-transform of  $\frac{8z^2}{(2z-1)(4z-1)}$ . b. (07 Marks) Solve the following difference equation using z-transforms: c.  $y_{n+2} + 2y_{n+1} + y_n = n$  with  $y_0 = y_1 = 0$ 

2 of 2

(06 Marks)

(06 Marks)